

# Lecture 15

(1)

$$\Omega_M \approx 0.3$$

$$\Omega_B = \Omega_{\text{stars}} + \Omega_{\text{gas, dust, ...}} \sim 0.05 \text{ (from}$$

Cosmic microwaves, and big bang nucleosynthesis,  
see later)

$$\Omega_M - \Omega_B \equiv \Omega_{\text{DM}} \quad \text{Dark matter!}$$

$$\Omega_{\text{DM}} \sim 0.25$$

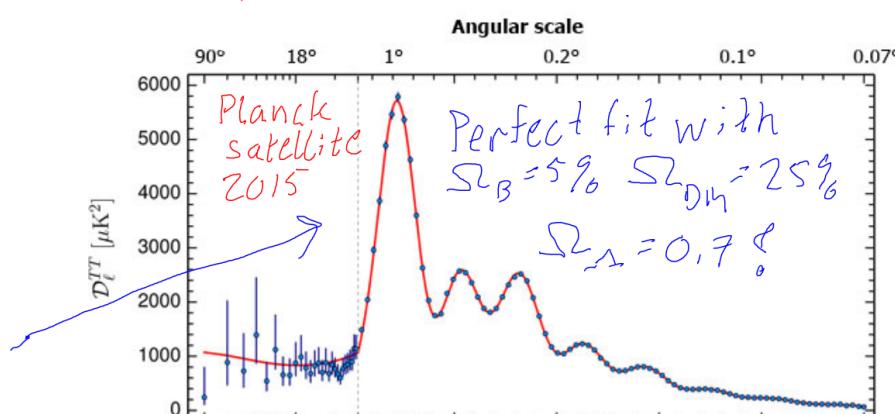
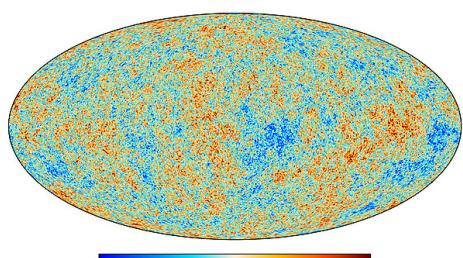
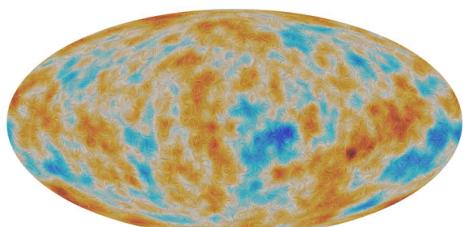
[Invisible matter would  
be a better name -  
has to be electrically  
neutral, otherwise would  
shine]

But what is  
it? Standard Model of particle physics  
has no good candidate (neutral, stable, ...)

⇒ non-baryonic matter

Indications for the existence of dark matter:

- CMB  $\Omega_{\text{DM}} \sim 25\%$
- Rotation curves of galaxies
- Gravitational lensing
- Big bang nucleosynthesis  $\Rightarrow \Omega_B \approx 5\%$



Angular correlations of temperature

## The early universe and the Cosmic Microwave Background

Friedmann:  $\frac{H^2}{H_0^2} = \left[ \underbrace{\Omega_m(1+z)^3}_{\equiv \Omega_m(z)} + \underbrace{\Omega_r(1+z)^4}_{\equiv \Omega_r(z)} + \underbrace{\Omega_k(1+z)^2}_{\equiv \Omega_k(z)} + \underbrace{\Omega_\Lambda}_{\equiv \Omega_\Lambda} \right]^{CMB}$

$$t=t_0 \Rightarrow z=0; \quad \Omega_m = 0.3, \quad \Omega_r \sim 10^{-5}, \quad \Omega_k < 10^{-3}, \quad \Omega_\Lambda = 0.7$$

$$\text{at } z=10^4 \quad \frac{\Omega_r(z)}{\Omega_m(z)} \sim \underbrace{\frac{\Omega_r}{\Omega_m}}_{\approx 10^{-4}} (1+10^4) \approx 1$$

This was the epoch of matter-radiation equality

For earlier times (larger  $z$ ), radiation dominated

CMB gives perfect Planck curve (COBE satellite measurements)

$$\Rightarrow f_r = \alpha_{rad} \cdot T^4 \sim T^4 \text{ (see formula sheet for } \alpha_{rad})$$

$$\text{But we also had } f_r \sim \left(\frac{a_0}{a}\right)^4 = (1+z)^4$$

$$\Rightarrow \text{temperature } T = T_0(1+z) \quad T_0 = 2.73 K$$

$$\text{At } z=10^4: \quad T = T_0(1+10^4) \approx 27000 K$$

Very hot, ionized plasma  $\Rightarrow$  rapid scattering of photons

As the universe expanded, it became cooler, and

at  $z \sim 1100$  [ $T \sim 3000 K$ ] it became transparent

to photons ("the surface of last scattering")

This light can still be seen, but due to redshift it

$$\text{is now at a temperature of } T_{CMB} = \frac{3000K}{1100} = 2.7 K$$

visible light  $\rightarrow$  microwaves, due to expansion!

$$\text{At } t=t_0, \quad T_{CMB} = 2.7 K \quad \langle E_r \rangle = 3k_B \cdot T_{CMB} \approx 7 \cdot 10^{-4} eV$$

Number density now,  $n_\gamma^0 = \frac{g_r(t_0)}{E_\gamma} \approx 360 \text{ cm}^{-3}$  (3)

$[g_r(t_0) = \alpha_{rad} T^4 = 7.565 \cdot 10^{-16} \text{ J m}^{-3} \text{ K}^{-4} \cdot (2.73 \text{ K})^4 = \frac{1}{1.602 \cdot 10^{-19} \text{ eV}} = 0.26 \text{ eV/cm}^3]$

we had  $\Omega_{\text{Baryon}} \approx 0.05$ ;  $f_c^0 \approx 0.5 \cdot 10^{-5} \text{ GeV/cm}^3$  [see formula sheet;  $h \approx 0.7$ ]

$$\Rightarrow f_B \approx 0.05 \cdot f_c^0 \text{ assume all is hydrogen}$$

$$\Rightarrow n_B = \frac{f_B}{m_H} \approx \frac{0.05 \cdot 0.5 \cdot 10^{-5} \text{ GeV cm}^{-3}}{1 \text{ GeV}} \approx 3 \cdot 10^{-7} \text{ cm}^{-3}$$

$$\Rightarrow \frac{n_B}{n_\gamma} \approx \frac{3 \cdot 10^{-7} \text{ cm}^{-3}}{360 \text{ cm}^{-3}} \approx 10^9$$

$\therefore 1 \text{ billion photons per nucleon!}$

[Side remark: Where did all the photons come from?]

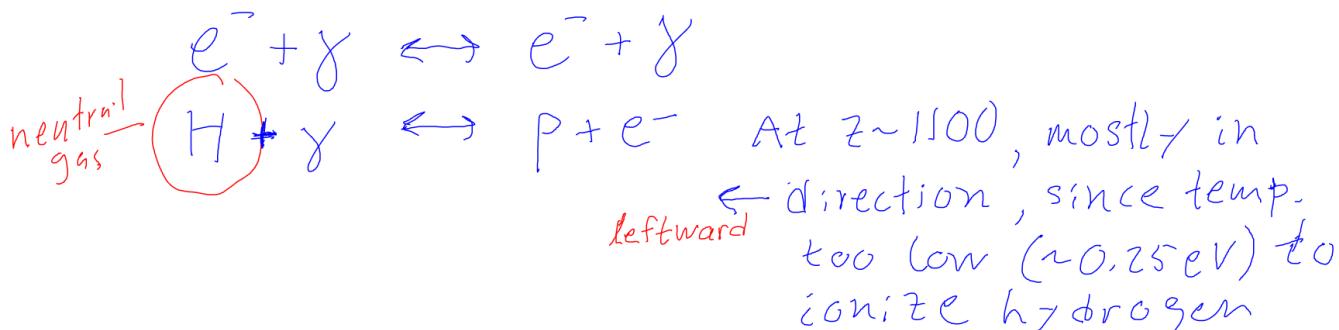
We don't know, but it probably was related to the mechanism that removed all antimatter in the universe:

$$10^9 \text{ antiparticles} + (10^9 + 1) \text{ particles} \rightarrow 1 \text{ particle} + 10^9 \text{ photons}$$

The  $10^9$  difference in numbers between particles and antiparticles is a violation of G and P, "CP violation".

How did the plasma become electrically neutral, and therefore transparent?

Processes at  $z \sim 10^4$ :



From  $z \sim 10^3$  (at  $t_{\text{decoupling}}$ ) until recently, the universe was matter dominated. (Equality at  $z \sim 10^4$ )

(4)

Matter domination

$$\Rightarrow a(t) \sim t^{2/3} \text{ (see lecture 13)}$$

$$\text{Now, } t_0 \approx 4 \cdot 10^{17} \text{ s (13 billion years)}$$

Estimate of  $t_{\text{dec}}$ :

$$T(t) = \frac{T_0}{a(t)} \left(= T_0 \cdot (1+z)\right)$$

$$\Rightarrow a(t) = \frac{T_0}{T(t)} = \left(\frac{t}{t_0}\right)^{2/3} \Rightarrow \frac{t_{\text{dec}}}{t_0} = \left(\frac{T_0}{T_{\text{dec}}}\right)^{\frac{3}{2}} = \left(\frac{2.7}{3000}\right)^{\frac{3}{2}}$$

$$\Rightarrow t_{\text{dec}} = t_0 \cdot \left(\frac{2.7}{3000}\right)^{\frac{3}{2}} = 1.1 \cdot 10^{13} \text{ s} = 340000 \text{ yrs}$$

                 X                 The earliest universe ( $z > 10^4$ ) was very simple:

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3} \rho_8 = \frac{8\pi G}{3} \alpha_{\text{rad}} T^4$$

Radiation domination  $\Rightarrow a(t) \sim \sqrt{t}$  (see lect. 13)

$$\Rightarrow H = \frac{\dot{a}}{a} = \frac{1}{2t}$$

$$\text{Thus } \left(\frac{1}{2t}\right)^2 = \frac{8\pi G_N}{3} \alpha_{\text{rad}} T^4 \Rightarrow \dots \Rightarrow$$

$$\Rightarrow T(\text{MeV}) \approx \frac{1}{\sqrt{t(\text{sec})}}$$

During radiation domination

Thus, 1 sec after the big bang, the temperature corresponded to 1 MeV (i.e.  $k_B \cdot T \sim 1 \text{ meV}$ )

$$k_B \sim 8.62 \cdot 10^{-5} \text{ eV/K} \Rightarrow T = 1 \text{ MeV} \leftrightarrow 10^{10} \text{ K}$$

(5)

## "Hot big bang"

$k_B T = 1 - 10 \text{ MeV}$  typical binding energy of nuclei

When  $k_B T$  was  $\gg 10 \text{ MeV}$  all processes were in (near) thermal equilibrium; when temperature was  $1 - 10 \text{ MeV}$  the distribution was near Maxwell-Boltzmann

$$n \sim (mc^2)^{3/2} e^{-\frac{mc^2}{k_B T}} \quad (mc^2 \gg E_{kin} \text{ at } 1 - 10 \text{ MeV})$$

$$\Rightarrow R_n \equiv \frac{n_n}{n_p} = \left( \frac{m_n}{m_p} \right)^{3/2} e^{-\frac{\Delta m c^2}{k_B T}} \quad \Delta m c^2 \approx 1.3 \text{ MeV}$$

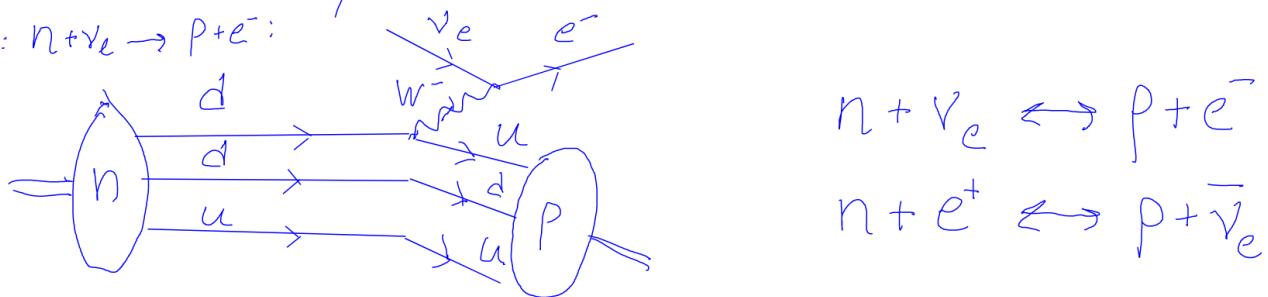
(see nuclear physics part)

$$\Rightarrow R_n \approx 1 \text{ for } k_B T > 1.3 \text{ MeV}$$

How can a neutron convert to a proton and vice versa?

Answer: Only weak interactions can do that!

Ex:  $n + \gamma_e \rightarrow p + e^-$ :



$$n + \gamma_e \leftrightarrow p + e^-$$

$$n + e^+ \leftrightarrow p + \bar{\nu}_e$$

(positrons are plentiful due to  $\gamma + \gamma \leftrightarrow e^+ + e^-$  etc.

$$\begin{array}{c} \gamma \rightarrow e^- \\ \gamma \rightarrow e^+ \end{array}$$

As temperature decreased to  $\sim \Delta m = 1.3 \text{ MeV}$

processes go faster to the right (as protons are lighter)

More exact calculation  $\Rightarrow k_B T \sim 0.8 \text{ MeV}$  when neutrons "freeze-out" (are not generated thermally)

$$\Rightarrow \frac{n_n}{n_p} \sim e^{-\frac{1.3 \text{ MeV}}{0.8 \text{ MeV}}} \approx \frac{1}{5} = 0.2 \text{ at } t \sim 1s$$

But neutrons can decay  $n \rightarrow p + e^- + \bar{\nu}_e \quad \tau_n \sim 880s$   
 $(\tau_{1/2} \sim 610s)$

(6)

Neutrons continue decaying, until they are "safe" inside stable nuclei



When  $t \sim 300\text{s}$ , all deuterons had become  ${}^3\text{He}$  or  ${}^4\text{He}$   
↓  
dominant

How many neutrons were there remaining?

$$\frac{n_n}{n_p} = \frac{1}{5} e^{-\frac{300s}{880s}} \sim \frac{1}{7}$$

$\uparrow$   
 $\tau/\tau_n$

~ all end up in helium,  ${}^4\text{He}$

So, for 2 neutrons there were 14 protons (ratio was 1:7),  $2n+2p$  give one helium nucleus  $\Rightarrow$  12 protons remaining. So for every  $2+14=16$  nucleons, 1 helium nucleus and 12 protons (hydrogen) are formed.

$\Rightarrow$  mass ratio (each  ${}^4\text{He}$  has 4 nucleons):

$$Y_{{}^4\text{He}} = \frac{4}{16} \sim 0.25 \quad (\text{More exact calculation} \Rightarrow Y_{{}^4\text{He}} \approx 0.24)$$

The rest is protons (i.e. hydrogen) plus very small amounts of Li, Be, D,  ${}^3\text{He}$  (no stable nuclei with mass 5 or 8)

$\Rightarrow$  Prediction of BBN (big bang nucleosynthesis):

The "primordial" gas in the universe consists of 24%  ${}^4\text{He}$ , 76% H (hydrogen) [Agrees very well with observations!]

$\Rightarrow$  strong evidence for Hot Big Bang

+ expansion (gives increasing T as  $t \rightarrow 0$ )

+ CMB (in microwaves, we "see" the Hot Big Bang!)