

# Lecture 3

- Antiparticles
- Leptons
- Quarks and hadrons
- The strong force

# Implications of introducing special relativity

Consider a particle of charge  $q$ , mass  $m$  with momentum  $p$  moving along the  $x$ -axis

What is its energy ?

Special relativity gives us a choice:  $E = \pm\sqrt{p^2c^2 + m^2c^4}$

$$E_+ = \sqrt{p^2c^2 + m^2c^4} \quad E_- = -\sqrt{p^2c^2 + m^2c^4}$$

Surely the negative energy solution is unphysical and daft.

Can't we just ignore it ?

No - from quantum mechanics, every observable must have a complete set of eigenstates. The negative energy states are needed to form that complete set.

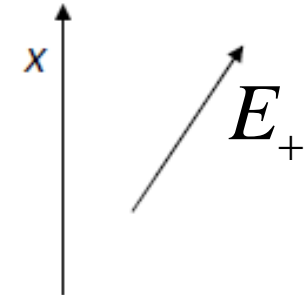
They must mean something....

# Negative energy states

Consider an electron moving in space along  $x$ -direction

Positive energy solution:  $\psi(x,t) = Ne^{-i\left(\frac{px-E_+t}{\hbar}\right)}$

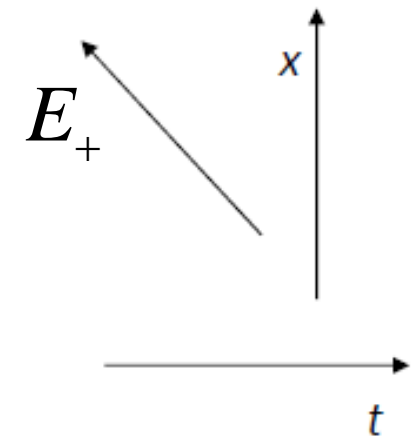
Moves to the right



Negative energy solution:

$$\psi(x,t) = Ne^{-i\left(\frac{px-E_-t}{\hbar}\right)} = Ne^{-i\left(\frac{px+E_+t}{\hbar}\right)} = Ne^{-i\left(\frac{px-E_+(-t)}{\hbar}\right)}$$

Moves to the left



⇒ Negative energy state moving forwards in time is equivalent to a positive energy state moving backwards in time.

What does a particle moving backwards in time look like ?

What are the implications of a particle (i.e. an observable state with positive energy) moving backwards in time ?

Lorentz force on an electron in a  $\vec{B}$ -field travelling forwards in time at a certain point in space and time  $\vec{r}$  and  $t$

$$\vec{F}(\vec{r}, t) = m \frac{d^2 \vec{r}}{dt^2} = q \vec{v} \times \vec{B} = -e \frac{d\vec{r}}{dt} \times \vec{B} \Rightarrow \frac{d^2 \vec{r}}{dt^2} = \frac{-e}{m} \frac{d\vec{r}}{dt} \times \vec{B}$$

Consider electron moving backwards in time ( $dt \rightarrow -dt$ ).

$$\frac{d^2 \vec{r}}{d(-t)^2} = \frac{-e}{m} \frac{d\vec{r}}{d(-t)} \times \vec{B} \Rightarrow \frac{d^2 \vec{r}}{dt^2} = \frac{+e}{m} \frac{d\vec{r}}{dt} \times \vec{B}$$

An electron moving backwards in time looks like a positively charged electron moving forwards in time!

# Antiparticles

Special relativity permits negative energy solutions and quantum mechanics demands we find a use for them.

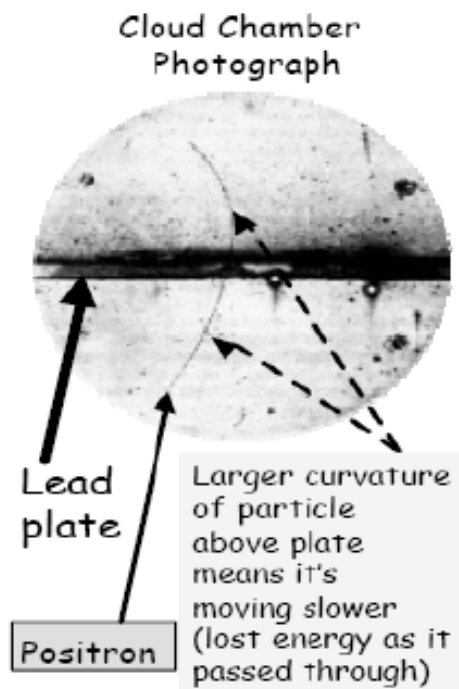
- (1) The wave function of a particle with negative energy moving forwards in time is the same as the wave function of a particle with positive energy moving backwards in time.
- (2) A positive energy particle with charge  $-q$  moving backwards in time looks like a positive energy particle with charge  $+q$  moving forwards in time.

We expect, for a given particle, to see the "same particle" but with opposite charge: *antiparticles*.

Antiparticles can be considered to be particles moving backwards in time - Feynman and Stueckelberg.

*Hole theory* (not covered) provides an alternative, though more old fashioned way of thinking about antiparticles.

# Electron and the positron



1897  $e^-$  discovered by J.J. Thompson

1932

Anderson measured the track of a cosmic ray particle in a magnetic field.

Same mass as an electron but positive charge

The positron ( $e^+$ ) - anti-particle of the electron

Nobel prize 1936

$B = 1.5T$  (out of page)

$\vec{F} = q(\vec{v} \times \vec{B})$  (to left)

$$r = \frac{p}{eB}$$

Every particle has an antiparticle.  
Some particles, eg photon, are their own antiparticles.

Special rules particles and antiparticles symbols and names.

# Feynman diagrams

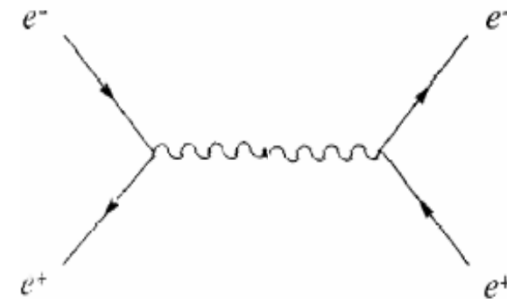
Important mathematical tool for calculating rates of processes - Feynman rules.

Qualitative treatment here

Represent any process by contributing diagrams.

One possible diagram for

$$e^+ + e^- \rightarrow e^+ + e^-$$



Strategy:

- (1) Build Feynman diagrams for electromagnetic processes
- (2) Consider how they can be used for simple rate estimates.
- (3) Show Feynman diagram formalism for other fundamental forces.



# Electromagnetic processes

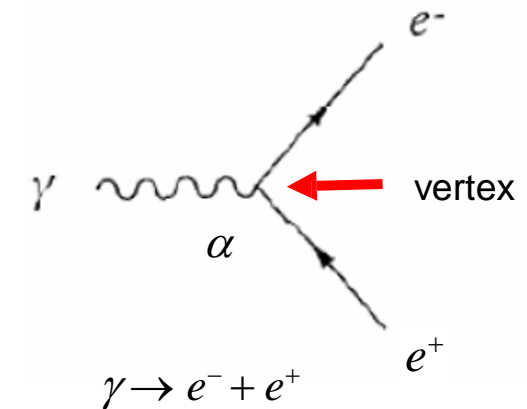
Convention - time flows to the right

The lines do not represent trajectories of a particle.

Arrow for antiparticle goes "backward in time".

Lines should not be taken as "trajectories" of particles

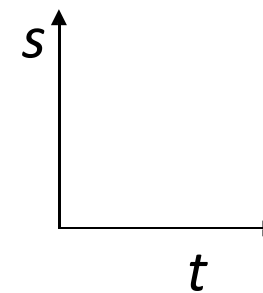
Interactions occur at a vertex.



A basic process.

Rule of thumb: a vertex carries a factor  $\alpha$  associated with the probability of that interaction taking place.

$$\alpha = \frac{1}{4\pi\epsilon_0} \frac{e^2}{\hbar c} \approx \frac{1}{137} \quad \text{Fine structure constant}$$



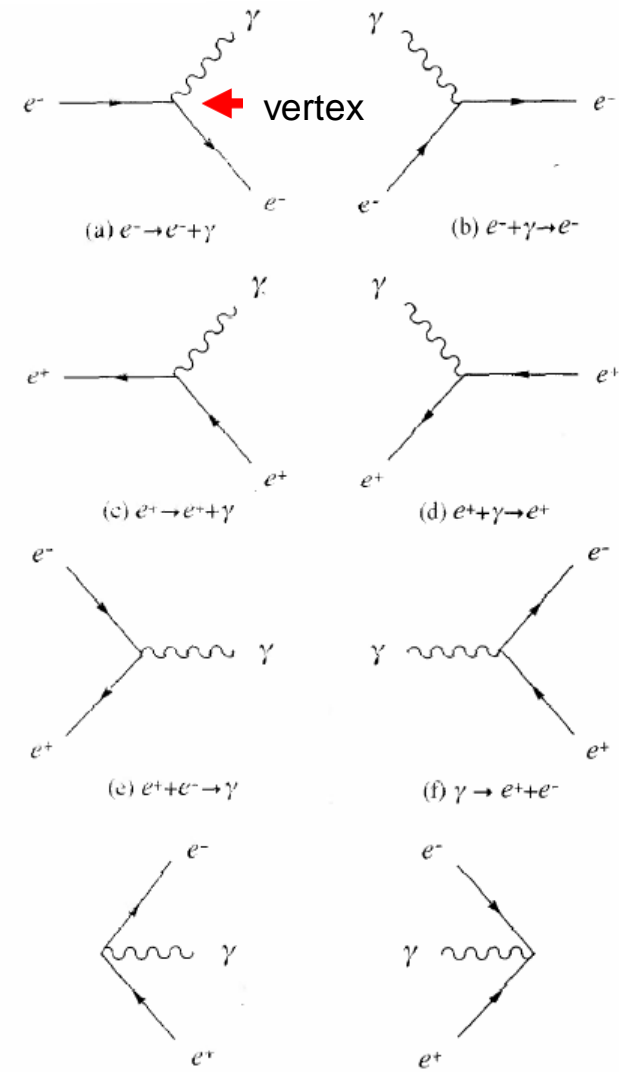
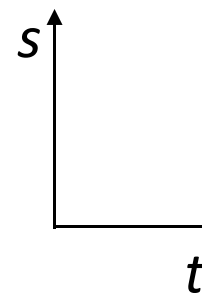
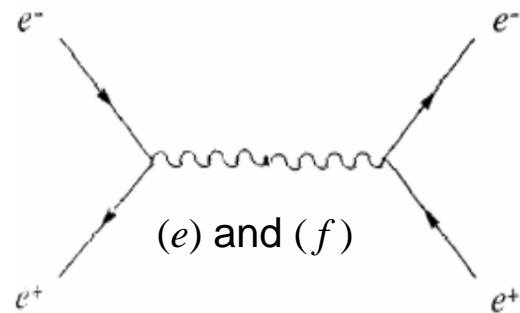
# Basic electromagnetic diagrams

Consider all electromagnetic processes built up from basic processes: (a) to (h)

The basic processes are never seen since they violate energy conservation (next slide)

They can be combined to make observable processes:

$$e^+ + e^- \rightarrow e^+ + e^-$$



## Using Feynman diagrams

$$e^+ + e^- \rightarrow \gamma + \gamma + \gamma$$

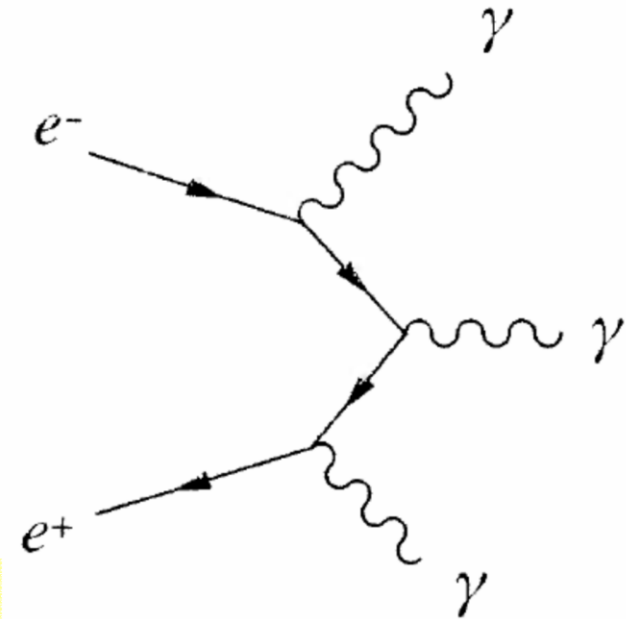
Three vertices  $\Rightarrow$  probability  $\propto \alpha^3$

$$R = \frac{\text{Rate}(e^+ + e^- \rightarrow \gamma + \gamma + \gamma)}{\text{Rate}(e^+ + e^- \rightarrow \gamma + \gamma)} \approx \frac{\alpha^3}{\alpha^2}$$
$$= \alpha = 0.7 \times 10^{-2}$$

Observed  $R \approx 10^{-3}$

$\Rightarrow$  Qualitative Feynman diagram picture gives suppression with (very) rough accuracy.

$\Rightarrow$  Full QED calculation gives correct rates.



+ other contributions

# Using Feynman diagrams

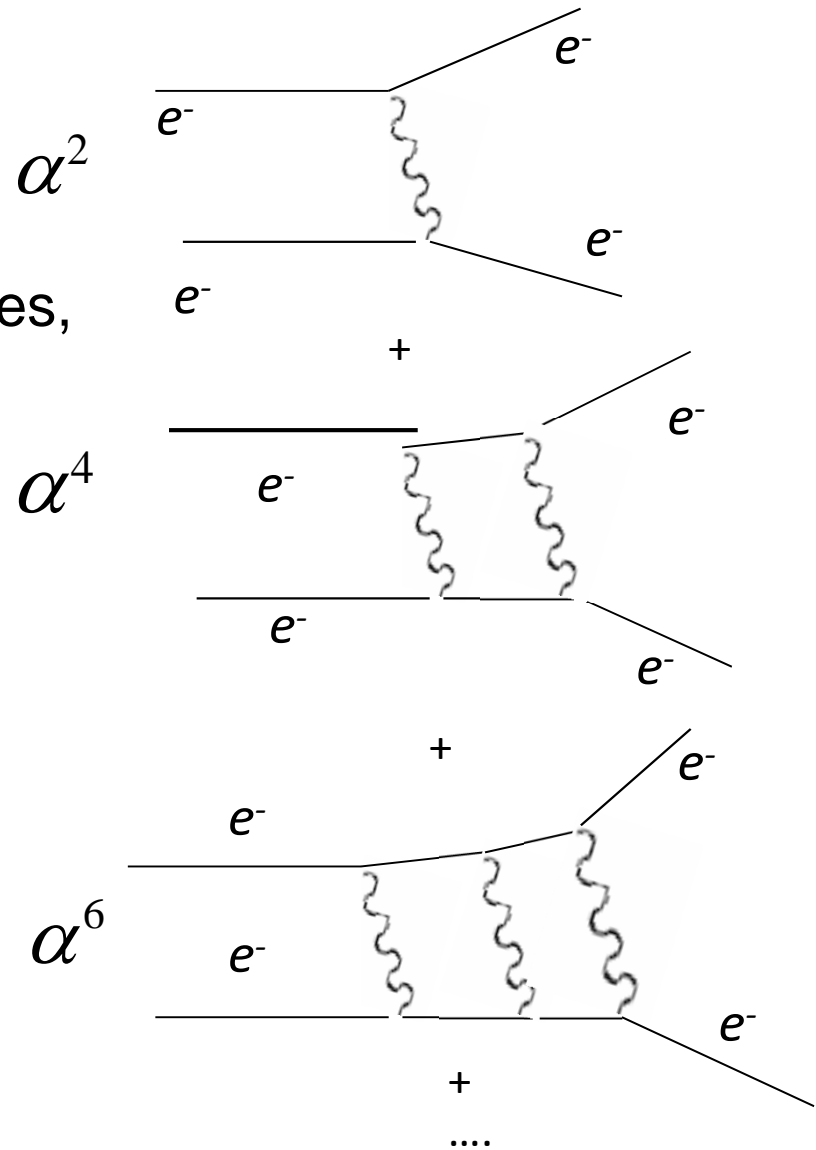
Two electrons are observed to repel

each other:  $e^- + e^- \rightarrow e^- + e^-$

Many different indistinguishable processes, eg one-photon, two-photon exchange, can contribute to the scattering

Coupling is weak  $\alpha \approx \frac{1}{137} \ll 1$

$\Rightarrow$  higher order processes contribute less and less to the calculation and can be safely be neglected in any approximate solution.



# The charged leptons

- Three types of charged lepton
- Electron, muon, tau
- $e^-$ ,  $e^+$ ,  $\mu^-$ ,  $\mu^+$ ,  $\tau^-$ ,  $\tau^+$
- Charged leptons interact via the weak and electromagnetic forces

Lepton	Charge ( $e$ )	Mass (GeV/ $c^2$ )
$e^-$	-1	0.0005
$\mu^-$	-1	0.105
$\tau^-$	-1	1.8

+ antiparticles

# Heavier leptons

- Muon  $\mu^-$  (Stevenson and Street, 1936)
- Measurements of energy loss of cosmic-ray particles.
- New particle with mass between  $e^-$  and  $p$  ( $106 \text{ MeV}/c^2$ )
- Interacts like a heavy electron

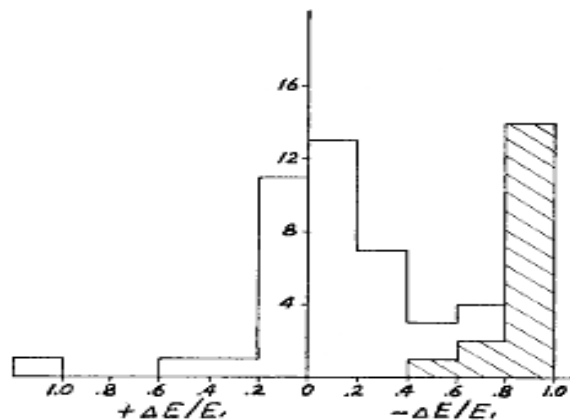
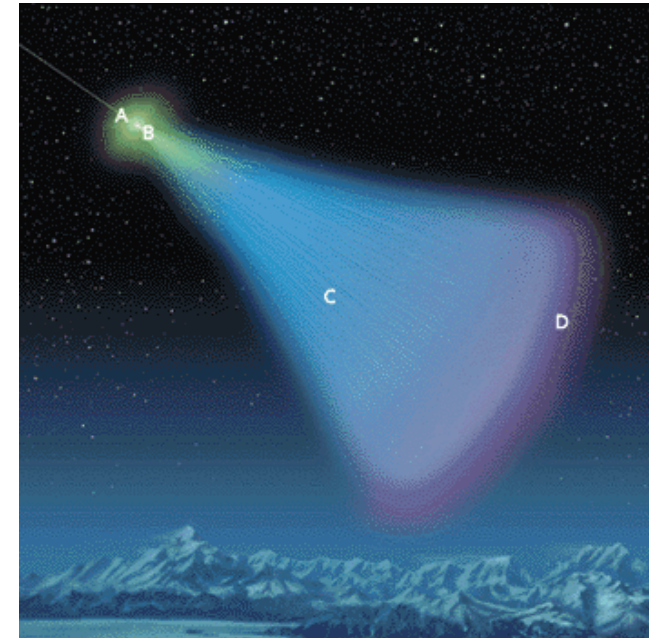
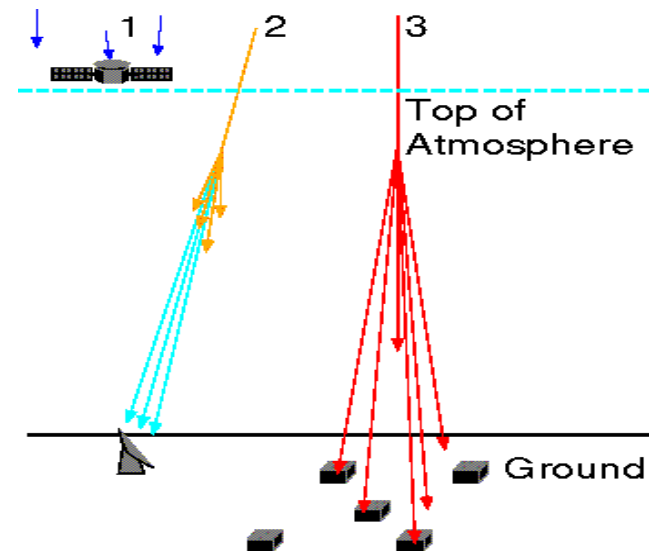
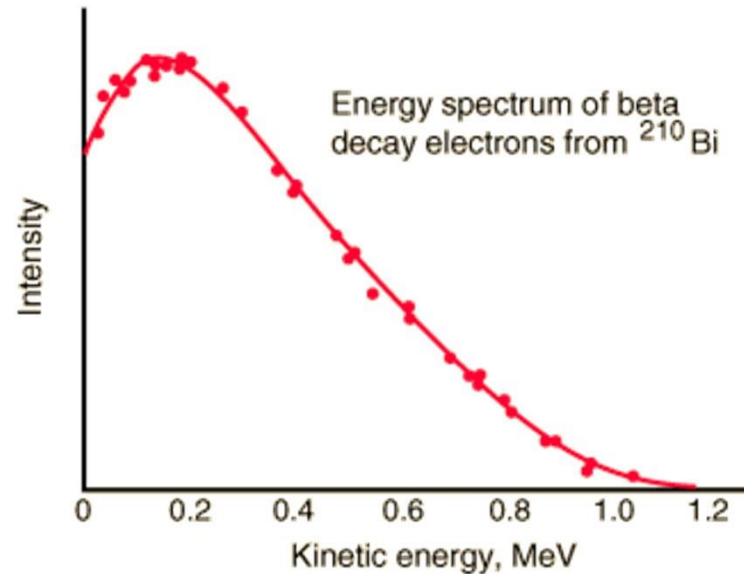
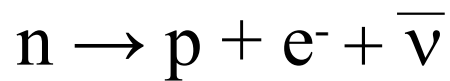
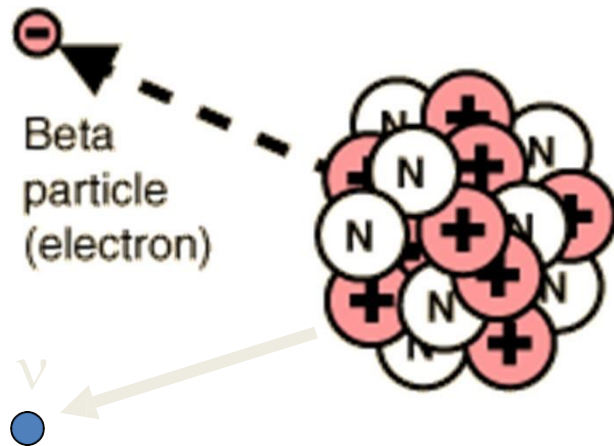


FIG. 2. Distribution of fractional losses in 1 cm of platinum.



# Evidence for neutrinos



- Electrons produced by beta decay do not all have the same energy.
  - Pauli proposed the existence of an unseen neutral particle to explain the observed electron spectrum.

# The lepton family

Spin 1/2

Lepton (antilepton)	Charge ( $e$ )	Mass (GeV/ $c^2$ )
$e^-$ ( $e^+$ )	-1 (+1)	0.0005
$\nu_e$ , ( $\bar{\nu}_e$ )	0	$\approx 0$
$\mu^-$ ( $\mu^+$ )	-1 (+1)	0.105
$\nu_\mu$ ( $\bar{\nu}_\mu$ )	0	$\approx 0$
$\tau^-$ ( $\tau^+$ )	-1 (+1)	1.8
$\nu_\tau$ ( $\bar{\nu}_\tau$ )	0	$\approx 0$

Charged leptons interact via the electromagnetic and weak forces.  
Neutrinos interact only via the weak force.



# Particles and antiparticles

Convention:

Charged leptons

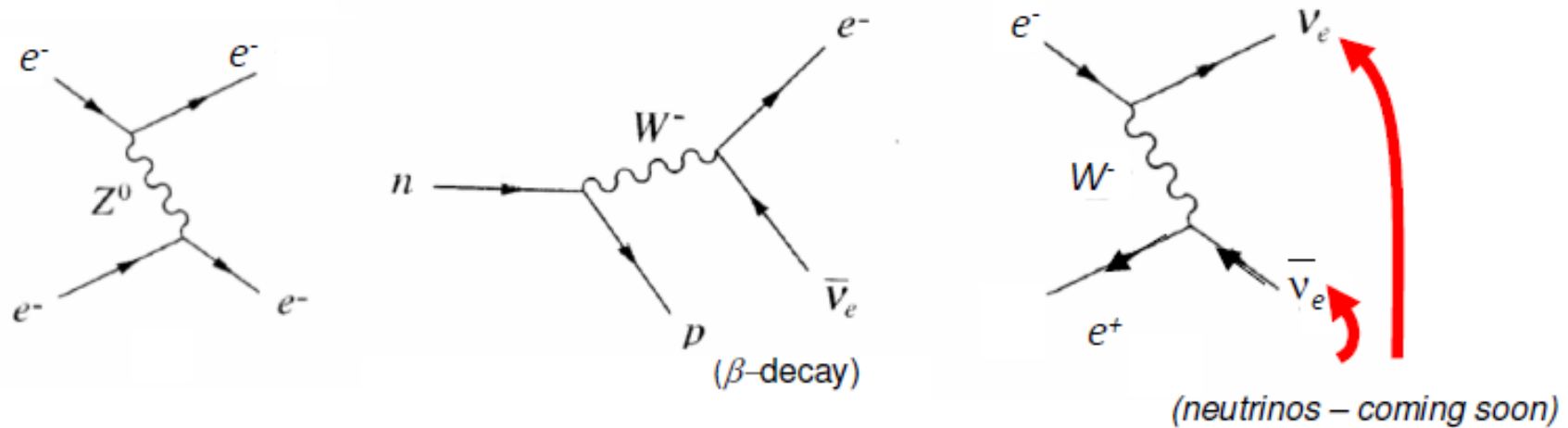
Tend to denote particles/antiparticles with charge:

[electron ( $e^-$ ), anti-electron i.e. positron ( $e^+$ )]

Neutral leptons use bars for antiparticles :

[electron neutrino ( $\nu_e$ ), anti-electron neutrino ( $\bar{\nu}_e$ )]

# The weak force



Use same formalism as for electromagnetic force

Very brief overview:

Exchange of 3 spin-1 particles:  $Z^0$  (mass=91.2 GeV/c<sup>2</sup>),  $W^+$ ,  $W^-$  (mass=80.4 GeV/c<sup>2</sup>)

$\Rightarrow$  range  $R_{w,z} \approx \frac{\hbar}{M_w c} \approx 2 \times 10^{-18} \text{m}$  (tiny - proton "radius"  $\approx 10^{-15} \text{m}$ )

Define coupling constant analogous to fine structure constant

$$\alpha_w = \frac{g_w^2}{4\pi\hbar c} \quad (1.39) \quad \alpha = \frac{e^2}{4\pi\epsilon_0\hbar c} \quad (1.24)$$

$g_w$  analogous to electric charge ( $\sim$  "weak charge")

$$\alpha_w = \frac{g_w^2}{4\pi\hbar c} \approx \frac{1}{240} \quad (1.41) \quad \left( \alpha \approx \frac{1}{137}, \text{ the weak force is only weak due to } W, Z \text{ masses} \right).$$

# Lepton number conservation

Leptons carry a conserved quantum number.

Flavour specific lepton numbers:

electron lepton number  $L_e$ , muon lepton number  $L_\mu$ , tau lepton number  $L_\tau$

(Obviously) for all other particles  $L_e = L_\mu = L_\tau = 0$

Lepton	$L_e$	$L_\mu$	$L_\tau$
$e^-$	1	0	0
$\nu_e$	1	0	0
$\mu^-$	0	1	0
$\nu_\mu$	0	1	0
$\tau^-$	0	0	1
$\nu_\tau$	0	0	1

Antileptons carry the opposite lepton number.

Eg  $\bar{\nu}_e, e^+, L_e = -1, L_\mu = L_\tau = 0$

Except for neutrino oscillations (to come) lepton number has never been seen to be violated.

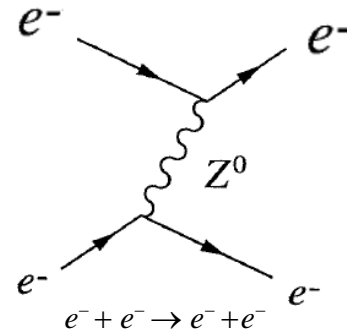
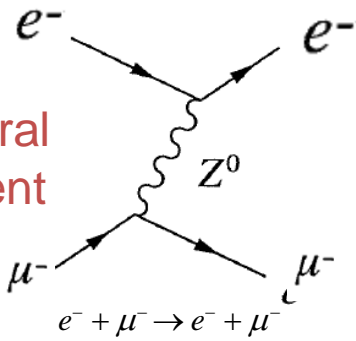
## Limits on lepton number violation in charged lepton decays

Decay	Violates	Limit on branching ratio
$\mu^- \rightarrow e^- + e^+ + e^-$	$L_\mu, L_e$	$< 1.0 \times 10^{-12}$
$\mu^- \rightarrow e^- + \gamma$	$L_\mu, L_e$	$< 1.2 \times 10^{-11}$
$\tau^- \rightarrow e^- + \gamma$	$L_\tau, L_e$	$< 1.1 \times 10^{-7}$
$\tau^- \rightarrow \mu^- + \gamma$	$L_\tau, L_\mu$	$< 6.8 \times 10^{-8}$
$\tau^- \rightarrow e^- + \mu^- + \mu^+$	$L_\tau, L_\mu$	$< 2 \times 10^{-7}$

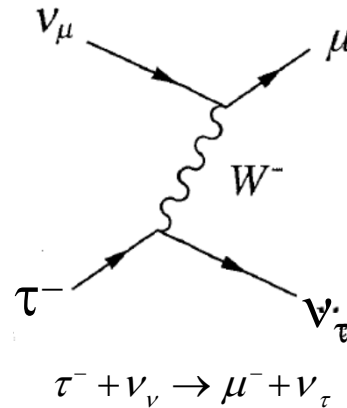
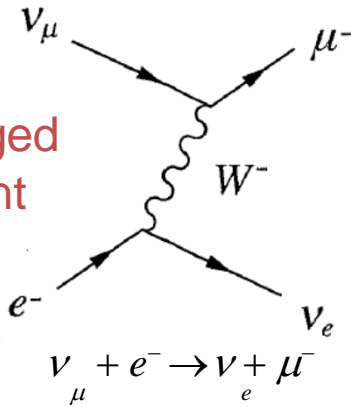
# Interactions of leptons

Leading order

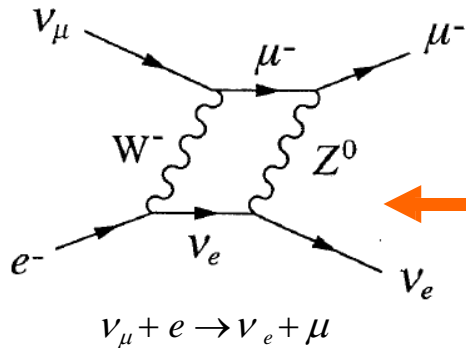
Neutral current



Charged current

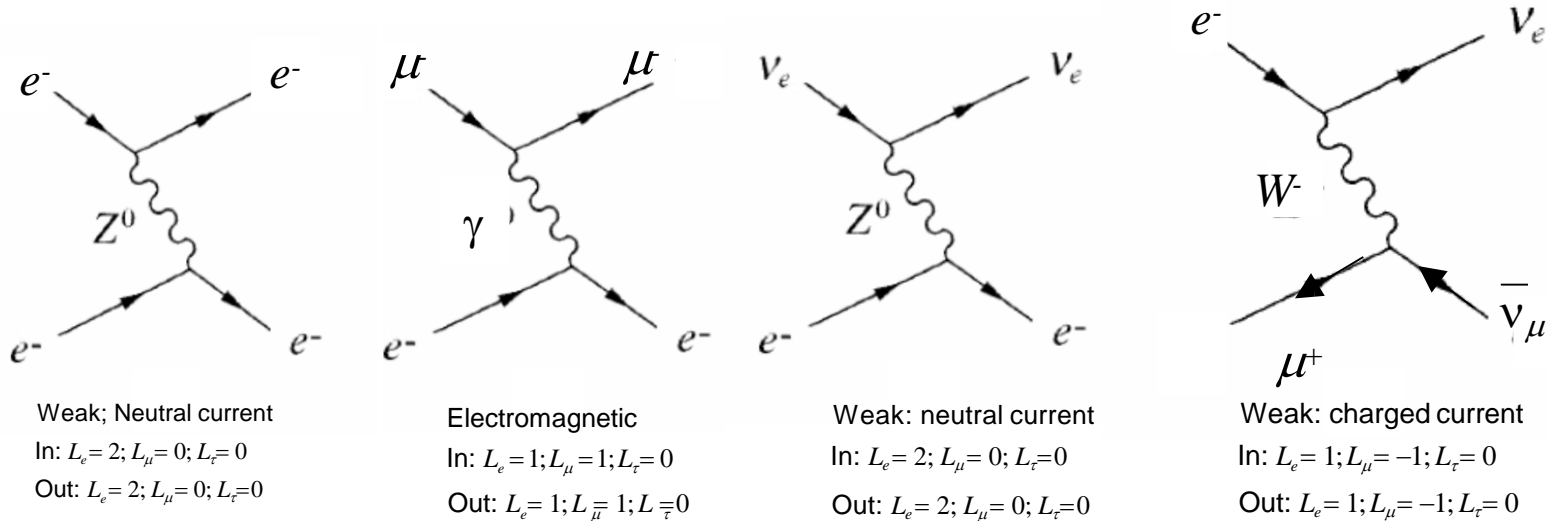


Higher order



← suppressed.

# Lepton interactions



Charged leptons interact via the *em* and weak forces.  
 Neutrinos only interact via the weak force.

Lepton number is always conserved at a vertex and in the whole process.

As for all forces:

*Charge conservation and energy-momentum conservation for incoming and outgoing particles.*

*Charge is conserved at a vertex though energy can appear to be violated when dealing with "internal lines" (lecture 1).*

# Question

Draw a Feynman diagram for a muon decay process.

# Question

Using Feynman diagrams explain why the reactions  $\nu_\mu + e^- \rightarrow \nu_\mu + e^-$  and  $\nu_\tau + e^- \rightarrow \nu_\tau + e^-$  are suppressed with respect to  $\nu_e + e^- \rightarrow \nu_e + e^-$ .



# The quarks

Quark	Q (e)	Mass (GeV $c^2$ )
<i>u- up</i>	$2/3$	$0.003$
<i>d- down</i>	$-1/3$	$0.005$
<i>s- strange</i>	$-1/3$	$0.15$
<i>c- charm</i>	$2/3$	$1.2$
<i>b- bottom</i>	$-1/3$	$4.2$
<i>t- top</i>	$2/3$	$171$

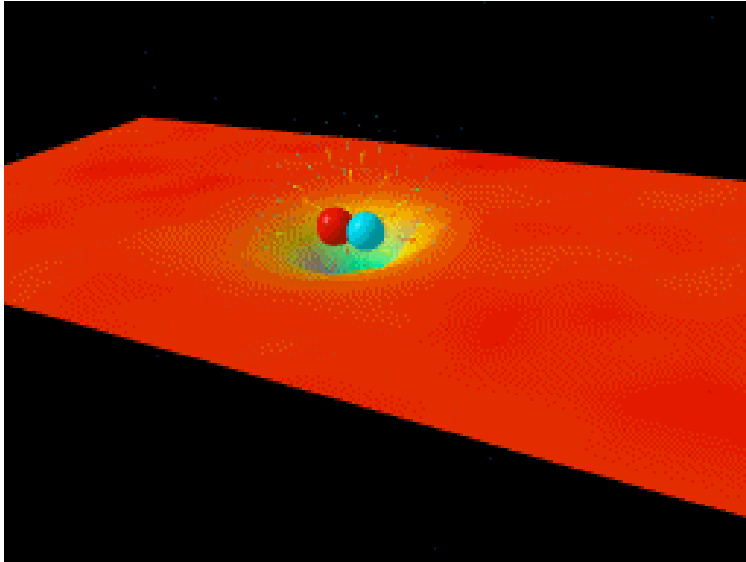
**Spin  $1/2$  particles**

Multiplets:

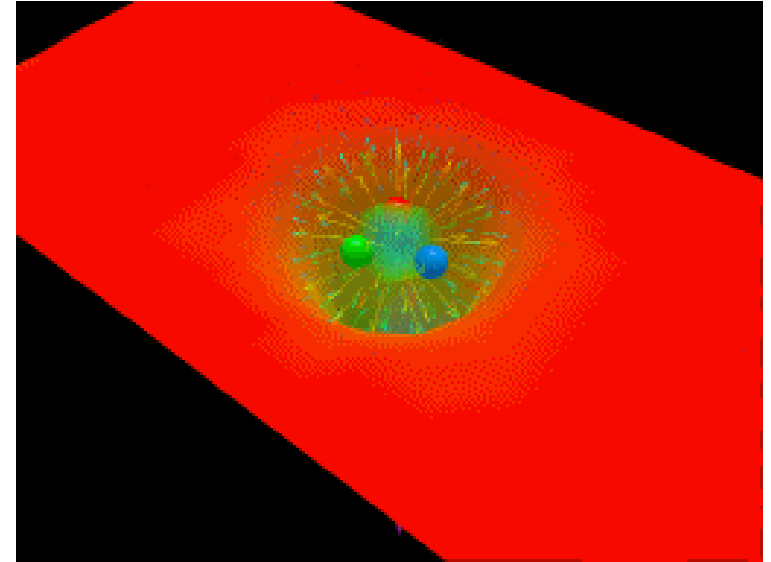
$$\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix}$$

+ antiquarks:  $\bar{u}, \bar{d}, \bar{s}, \bar{c}, \bar{b}, \bar{t}$  opposite charge:  $Q \rightarrow -Q$

# Mesons and baryons



Meson  
(quark-antiquark)



Baryons  
(quark-quark-quark)

Strong force is a short range ( $\sim 1\text{fm}$ ) force which acts to confine quarks and antiquarks in hadrons. "Bare" quarks are not seen.

# Hadrons

Two types: mesons (quark+antiquark) and baryons (quark+quark+quark)

PSEUDOSCALAR MESONS (Spin 0)

Meson	Quark content	Charge	Mass	Lifetime	Principal decays
$\pi^+$	$u\bar{d}, d\bar{u}$	+1, -1	135.569	$2.60 \times 10^{-8}$	$\mu\nu_\mu$
$\pi^0$	$(u\bar{u} - d\bar{d})/\sqrt{2}$	0	134.964	$8.7 \times 10^{-17}$	$\gamma\gamma$
$K^\pm$	$u\bar{s}, s\bar{u}$	+1, -1	493.67	$1.24 \times 10^{-8}$	$\mu\nu_\mu, \pi^+\pi^0, \pi^+\pi^-\pi^0$
$K^0, \bar{K}^0$	$d\bar{s}, s\bar{d}$	0, 0	497.72	$\left\{ \begin{array}{l} K_S^0 0.892 \times 10^{-10} \\ K_L^0 5.18 \times 10^{-8} \end{array} \right.$	$\pi^+\pi^-, \pi^0\pi^0$
$\eta$	$(u\bar{u} + d\bar{d} - 2s\bar{s})/\sqrt{6}$	0	548.8	$7 \times 10^{-19}$	$\pi e\nu_e, \pi\mu\nu_\mu, \pi\pi\pi$
$\eta'$	$(u\bar{u} + d\bar{d} + s\bar{s})/\sqrt{3}$	0	957.6	$3 \times 10^{-21}$	$\gamma\gamma, \pi^0\pi^0\pi^0, \pi^+\pi^-\pi^0$
$D^\pm$	$c\bar{d}, d\bar{c}$	+1, -1	1869	$9 \times 10^{-13}$	$K\pi\pi$
$D^0, \bar{D}^0$	$c\bar{u}, u\bar{c}$	0, 0	1865	$4 \times 10^{-13}$	$K\pi\pi$
$F^\pm$ (now $D_s^\pm$ )	$c\bar{s}, s\bar{c}$	+1, -1	1971	$3 \times 10^{-13}$	not established
$B^\pm, \bar{B}^0$	$u\bar{b}, b\bar{u}$	+1, -1	5271	$14 \times 10^{-13}$	$D + ?$
$B^0, \bar{B}^0$	$d\bar{b}, b\bar{d}$	0, 0	5275		
$\eta_c$	$c\bar{c}$	0	2981	$6 \times 10^{-23}$	$KK\pi, \eta\pi\pi, \eta'\pi\pi$

BARYONS (Spin  $\frac{1}{2}$ )

Baryon	Quark content	Charge	Mass	Lifetime	Principal decays
$N$ $\left\{ \begin{array}{l} p \\ n \end{array} \right.$	$uud$ $udd$	+1 0	938.280 939.573	$\infty$ 900	— $p\bar{e}\bar{\nu}_e$
$\Lambda$	$uds$	0	1115.6	$2.63 \times 10^{-10}$	$p\pi^-, n\pi^0$
$\Sigma^+$	$uus$	+1	1189.4	$0.80 \times 10^{-10}$	$p\pi^0, n\pi^+$
$\Sigma^0$	$uds$	0	1192.5	$6 \times 10^{-20}$	$\Delta\gamma$
$\Sigma^-$	$dds$	-1	1197.3	$1.48 \times 10^{-10}$	$n\pi^-$
$\Xi^0$	$uss$	0	1314.9	$2.90 \times 10^{-10}$	$\Delta\pi^0$
$\Xi^-$	$dss$	-1	1321.3	$1.64 \times 10^{-10}$	$\Delta\pi^-$
$\Lambda_c^+$	$udc$	+1	2281	$2 \times 10^{-13}$	not established

VECTOR MESONS (Spin 1)

Meson	Quark content	Charge	Mass	Lifetime	Principal decays
$\rho$	$u\bar{d}, d\bar{u}, (u\bar{u} - d\bar{d})/\sqrt{2}$	+1, -1, 0	770	$0.4 \times 10^{-23}$	$\pi\pi$
$K^*$	$u\bar{s}, s\bar{u}, d\bar{s}, s\bar{d}$	+1, -1, 0, 0	892	$1 \times 10^{-23}$	$K\pi$
$\omega$	$(u\bar{u} + d\bar{d})/\sqrt{2}$	0	783	$7 \times 10^{-23}$	$\pi^+\pi^-\pi^0, \pi^0\gamma$
$\phi$	$s\bar{s}$	0	1020	$20 \times 10^{-23}$	$K^+K^-, K^0\bar{K}^0$
$J/\psi$	$c\bar{c}$	0	3097	$1 \times 10^{-20}$	$e^+e^-, \mu^+\mu^-, 5\pi, 7\pi$
$D^*$	$c\bar{d}, d\bar{c}, c\bar{u}, u\bar{c}$	+1, -1, 0, 0	2010	$>1 \times 10^{-22}$	$D\pi, D\gamma$
$\Upsilon$	$b\bar{b}$	0	9460	$2 \times 10^{-20}$	$\tau^+\tau^-, \mu^+\mu^-, e^+e^-$

BARYONS (Spin  $\frac{3}{2}$ )

Baryon	Quark content	Charge	Mass	Lifetime	Principal decays
$\Delta$	$uuu, uud, udd, ddd$	+2, +1, 0, -1	1232	$0.6 \times 10^{-23}$	$N\pi$
$\Sigma^*$	$uus, uds, dds$	+1, 0, -1	1385	$2 \times 10^{-23}$	$\Delta\pi, \Sigma\pi$
$\Xi^*$	$uss, dss$	0, -1	1533	$7 \times 10^{-23}$	$\Xi\pi$
$\Omega^-$	$sss$	-1	1672	$0.82 \times 10^{-10}$	$\Delta K^-, \Xi^0\pi^-, \Xi^-\pi^0$

Full particle listings from the  
*Review of Particle Physics:*

[http://pdg.lbl.gov/2008/listings/contents\\_listings.html](http://pdg.lbl.gov/2008/listings/contents_listings.html)

# Hadron quantum numbers

## Mesons (bosons)

Particle	Mass (MeV)	$B$	$Q$	$S$	$C$	$\bar{B}$
$\pi^+$ ( $u\bar{d}$ )	140	0	1	0	0	0
$K^-$ ( $s\bar{u}$ )	494	0	-1	-1	0	0
$D^-$ ( $\bar{c}d$ )	1869	0	-1	0	-1	0
$D_s^+$ ( $c\bar{s}$ )	1971	0	1	0	1	0
$\Upsilon$ ( $b\bar{b}$ )	9460	0	0	0	0	0

## Baryons (fermions)

Particle	Mass (MeV)	$B$	$Q$	$S$	$C$	$\bar{B}$
$p$ ( $uud$ )	938	1	1	0	0	0
$n$ ( $udu$ )	940	1	0	0	0	0
$\Lambda$ ( $uds$ )	1116	1	0	-1	0	0
$\Lambda_c$ ( $udc$ )	2285	1	1	0	1	0
$\Lambda_b$ ( $udb$ )	5624	1	0	0	0	-1

# Particles and antiparticles

Hadrons:

Baryons use a bar [proton  $p(uud)$ , antiprotons  $\bar{p}(\bar{u}\bar{u}\bar{d})$ ]

Mesons are quark-antiquark i.e. matter-antimatter.

⇒ There are no "anti-mesons"

Can, however, swap quark → antiquark, antiquark → quark

Eg  $K^0(d\bar{s}) \rightarrow \bar{K}^0(\bar{d}s)$  (use bar for neutral mesons)

$K^+(u\bar{s}) \rightarrow K^-(\bar{u}s)$  (use charge)

Some neutral particles are their own antiparticle:

Eg  $\gamma, \pi^0$

# The quarks

Spin  $\frac{1}{2}$  particles

+ antiparticles

Quark	Q (e)	Mass (GeV/c <sup>2</sup> )	B	S	C	$\bar{B}$	T
<i>u- up</i>	2/3	0.003	1/3	0	0	0	0
<i>d- down</i>	-1/3	0.005	1/3	0	0	0	0
<i>s- strange</i>	-1/3	0.15	1/3	-1	0	0	0
<i>c- charm</i>	2/3	1.2	1/3	0	1	0	0
<i>b- bottom</i>	-1/3	4.2	1/3	0	0	-1	0
<i>t- top</i>	2/3	171	1/3	0	0	0	1

For antiquarks: internal quantum numbers change sign.

Charge:  $Q \rightarrow -Q$ , Baryon number:  $B \rightarrow -B$

Flavour: (strangeness)  $S \rightarrow -S$ , ("charmness")  $C \rightarrow -C$ , ("bottomness")  $\bar{B} \rightarrow -\bar{B}$ ,  $T \rightarrow -T$

Charge is always conserved.

Flavour quantum numbers are conserved in strong and electromagnetic decays but need not be conserved in weak decays.

# Hadron flavour quantum numbers

General rule for all hadrons.

Total strangeness  $S = \sum$  strangeness

$$= N_{\bar{s}} - N_s = (\text{no. } \bar{s} \text{ quarks} - \text{no. } s \text{ quarks})$$

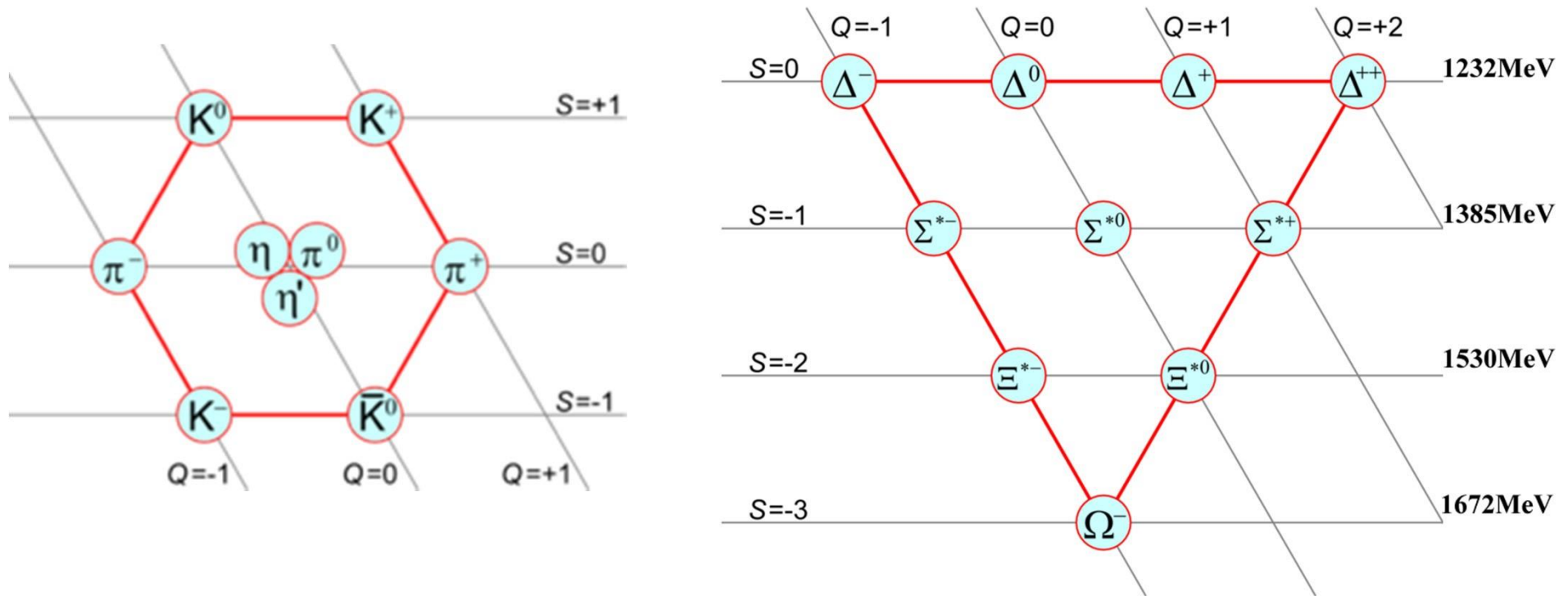
Similarly  $C = N_c - N_{\bar{c}}$  ;  $\bar{B} = N_{\bar{b}} - N_b$  (obs! No "top" hadrons)

Baryon number:  $B = \sum$  quark-baryon-number

$$\text{Eg proton } (uud) : S = C = \bar{B} = 0 \quad , \quad B = 3 \times \frac{1}{3} = 1$$

$$K^+ (u\bar{s}) : S = 1, C = \bar{B} = 0 \quad , \quad B = \frac{1}{3} - \frac{1}{3} = 0$$

# Evidence for quarks



Periodic structure of hadrons ( $SU(3)$  multiplets).



# Evidence for a new quantum number: colour

$$\Omega^- : 3 \text{ strange quarks, spin } 3/2 \quad \uparrow\uparrow\uparrow$$
$$\psi = \psi_{space} \psi_{spin} \psi_{flavour} \psi_{colour} \quad (4.03)$$

Need an extra quantum number (colour) to distinguish quarks to ensure anti-symmetric wave-function and Pauli's exclusion principle.

# Hadrons and the strong force

The strong force occurs between particles carrying "colour" charge.

Range of the strong force  $\approx 10^{-15}\text{m}$ .

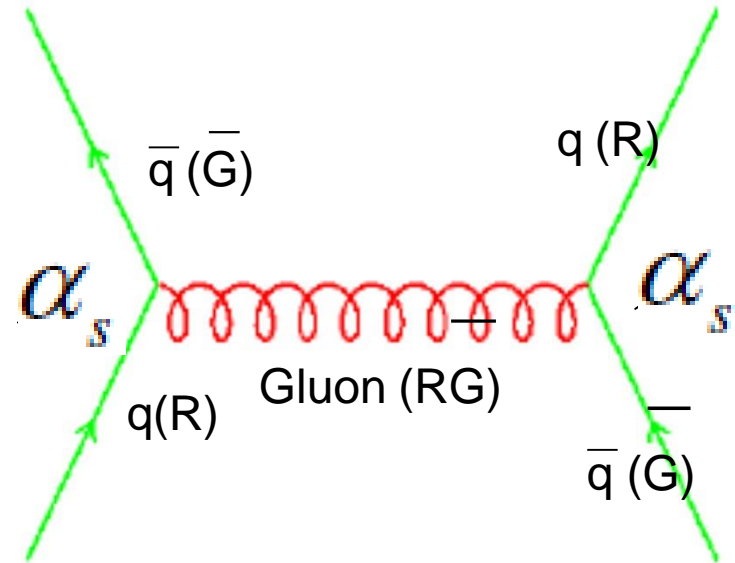
Coupling at a vertex:  $\alpha_s$

A quark can carry 3 colours: Red (R), Green (G), Blue (B)

There are eight gluons:

Gluons themselves carry colour and self-interact:

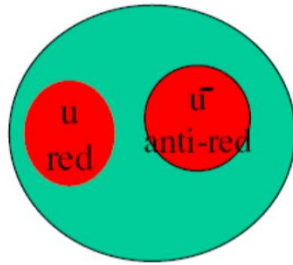
$$|R\bar{G}\rangle, |R\bar{B}\rangle, |G\bar{R}\rangle, |G\bar{B}\rangle, |B\bar{R}\rangle, |B\bar{G}\rangle, \frac{1}{\sqrt{2}}(R\bar{R}-G\bar{G}), \frac{1}{\sqrt{6}}(R\bar{R}+G\bar{G}-2B\bar{B})$$



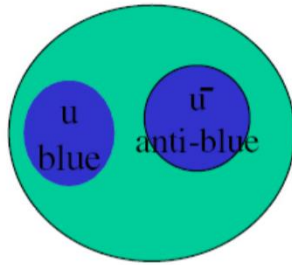
The theory of the strong force is quantum chromodynamics (QCD).

# Colour combinations

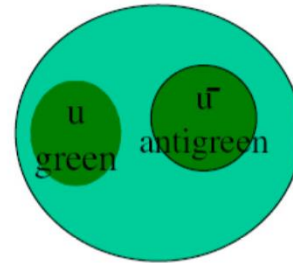
A meson has a colour-anticolour pair=white (colour singlet)



$\pi^0$

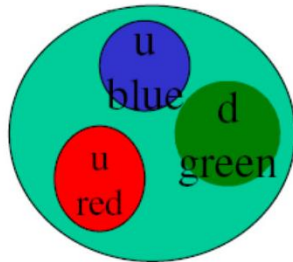


$\pi^0$



$\pi^0$

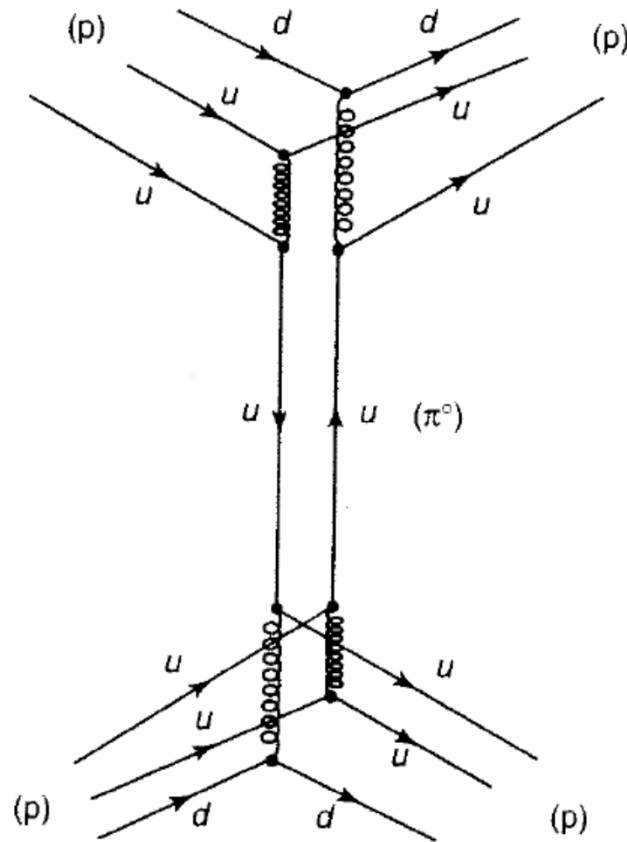
A baryon has red, blue, green triplet=white (colour singlet)



p

We have never seen a quark or gluon!  
Nature abhors naked colour.  
Every particle in nature is colourless/colour singlet

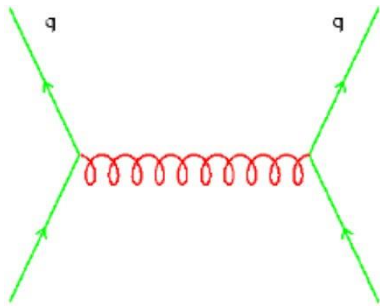
# QCD Description of the Strong Nuclear Force



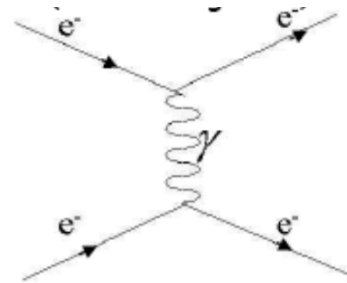
Yukawa model proposed pion exchange  
Interaction results from internal gluon lines and  
quark exchange

# The fundamental forces

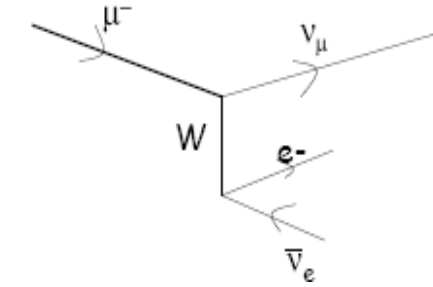
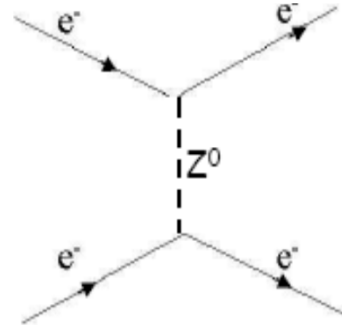
Different exchange particles mediate the forces:



strong



electromagnetic



weak

Interaction	Relative strength	Range	Exchange	Mass (GeV)	Charge	Spin
Strong	1	Short ( $\approx 10^{-16}$ m)	Gluon	0	0	1
Electromagnetic	$1/137$	Long ( $1/r^2$ )	Photon	0	0	1
Weak	$10^{-9}$	Short ( $\approx 10^{-16}$ m)	$W^+, W^-, Z$	80.4, 80.4, 91.2	+e, -e, 0	1
Gravitational	$10^{-38}$	Long ( $1/r^2$ )	Graviton ?	0	0	2

No quantum field theory yet for gravity

# Standard Model of Elementary Particles

		three generations of matter (fermions)				
		I	II	III	Next lecture	
mass		$\approx 2.4 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 172.44 \text{ GeV}/c^2$	0	$\approx 125.09 \text{ GeV}/c^2$
charge		$2/3$	$2/3$	$2/3$	0	0
spin		$1/2$	$1/2$	$1/2$	1	0
		<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> Higgs
	<b>QUARKS</b>	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
		$-1/3$	$-1/3$	$-1/3$	0	
		$1/2$	$1/2$	$1/2$	1	
		<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b><math>\gamma</math></b> photon	
		$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.67 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	$\approx 91.19 \text{ GeV}/c^2$	
		-1	-1	-1	0	
		$1/2$	$1/2$	$1/2$	1	
		<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau	<b>Z</b> Z boson	
	<b>LEPTONS</b>	$< 2.2 \text{ eV}/c^2$	$< 1.7 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$\approx 80.39 \text{ GeV}/c^2$	
		0	0	0	$\pm 1$	
		$1/2$	$1/2$	$1/2$	1	
		<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino	<b>W</b> W boson	
						<b>SCALAR BOSONS</b>
						<b>GAUGE BOSONS</b>

# Particles in nature

**PARTICLE DATA**  
(Mass in MeV/c<sup>2</sup>; Lifetime in Seconds; Charge in Units of Proton Charge.)

**QUARKS (Spin 1/2)**

	Flavor	Charge	Mass (speculative)		
			Bare	Effective	
				In baryons	In mesons
First generation	<i>d</i>	-1/3	7.5	363	310
	<i>u</i>	+2/3	4.2		
Second generation	<i>s</i>	-1/3	150	538	483
	<i>c</i>	+2/3	1100		
Third generation	<i>b</i>	-1/3	4200	1500	4700
	<i>t</i>	+2/3	175000		

**LEPTONS (Spin 1/2)**

	Lepton	Charge	Mass	Lifetime	Principal decays
First generation	<i>e</i>	-1	0.511003	∞	—
	<i>ν<sub>e</sub></i>	0	small	∞	—
Second generation	<i>μ</i>	-1	105.659	2.197 × 10 <sup>-6</sup>	<i>eν<sub>μ</sub>ν̄<sub>e</sub></i>
	<i>ν<sub>μ</sub></i>	0	small	∞	—
Third generation	<i>τ</i>	-1	1784	3.3 × 10 <sup>-13</sup>	<i>μν<sub>μ</sub>ν̄<sub>μ</sub>, eν<sub>μ</sub>ν̄<sub>e</sub>, ρν<sub>τ</sub></i>
	<i>ν<sub>τ</sub></i>	0	small	∞	—

**MEDIATORS (Spin 1)**

Mediator	Charge	Mass	Lifetime	Force
gluon	0	0	∞	strong
photon (γ)	0	0	∞	electromagnetic
W <sup>±</sup>	±1	81,800	unknown	(charged) weak
Z <sup>0</sup>	0	92,600	unknown	(neutral) weak

**BARYONS (Spin 1/2)**

Baryon	Quark content	Charge	Mass	Lifetime	Principal decays
<i>N</i> { <i>p</i> , <i>n</i> }	<i>uud</i>	+1	938.280	∞	—
	<i>udd</i>	0	939.573	900	<i>pēν<sub>e</sub></i>
<i>Λ</i>	<i>uds</i>	0	1115.6	2.63 × 10 <sup>-10</sup>	<i>pπ<sup>-</sup>, nπ<sup>0</sup></i>
<i>Σ<sup>+</sup></i>	<i>uus</i>	+1	1189.4	0.80 × 10 <sup>-10</sup>	<i>pπ<sup>0</sup>, nπ<sup>+</sup></i>
<i>Σ<sup>0</sup></i>	<i>uds</i>	0	1192.5	6 × 10 <sup>-20</sup>	<i>Λγ</i>
<i>Σ<sup>-</sup></i>	<i>dds</i>	-1	1197.3	1.48 × 10 <sup>-10</sup>	<i>nπ<sup>-</sup></i>
<i>Ξ<sup>0</sup></i>	<i>uss</i>	0	1314.9	2.90 × 10 <sup>-10</sup>	<i>Λπ<sup>0</sup></i>
<i>Ξ<sup>-</sup></i>	<i>dss</i>	-1	1321.3	1.64 × 10 <sup>-10</sup>	<i>Λπ<sup>-</sup></i>
<i>Λ<sub>c</sub><sup>+</sup></i>	<i>udc</i>	+1	2281	2 × 10 <sup>-13</sup>	not established

**BARYONS (Spin 3/2)**

Baryon	Quark content	Charge	Mass	Lifetime	Principal decays
<i>Δ</i>	<i>uuu, uud, udd, ddd</i>	+2, +1, 0, -1	1232	0.6 × 10 <sup>-23</sup>	<i>Nπ</i>
<i>Σ*</i>	<i>uus, uds, dds</i>	+1, 0, -1	1385	2 × 10 <sup>-23</sup>	<i>Λπ, Σπ</i>
<i>Ξ*</i>	<i>uss, dss</i>	0, -1	1533	7 × 10 <sup>-23</sup>	<i>Ξπ</i>
<i>Ω<sup>-</sup></i>	<i>sss</i>	-1	1672	0.82 × 10 <sup>-10</sup>	<i>ΛK<sup>-</sup>, Ξ<sup>0</sup>π<sup>-</sup>, Ξ<sup>-</sup>π<sup>0</sup></i>

**PSEUDOSCALAR MESONS (Spin 0)**

Meson	Quark content	Charge	Mass	Lifetime	Principal decays	
<i>π<sup>±</sup></i>	<i>uđ, dū</i>	+1, -1	139.569	2.60 × 10 <sup>-8</sup>	<i>μν<sub>μ</sub></i>	
<i>π<sup>0</sup></i>	<i>(uū - dđ)/√2</i>	0	134.964	8.7 × 10 <sup>-17</sup>	<i>γγ</i>	
<i>K<sup>±</sup></i>	<i>uš, sū</i>	+1, -1	493.67	1.24 × 10 <sup>-8</sup>	<i>μν<sub>μ</sub>, π<sup>±</sup>π<sup>0</sup>, π<sup>±</sup>π<sup>±</sup>π<sup>∓</sup></i>	
<i>K<sup>0</sup>, K̄<sup>0</sup></i>	<i>dš, sđ</i>	0, 0	497.72	<i>K<sup>0</sup><sub>S</sub></i>	0.892 × 10 <sup>-10</sup>	<i>π<sup>±</sup>π<sup>∓</sup>, π<sup>0</sup>π<sup>0</sup></i>
				<i>K<sup>0</sup><sub>L</sub></i>	5.18 × 10 <sup>-8</sup>	<i>πeν<sub>e</sub>, πμν<sub>μ</sub>, πππ</i>
<i>η</i>	<i>(uū + dđ - 2sš)/√6</i>	0	548.8	7 × 10 <sup>-19</sup>	<i>γγ, π<sup>0</sup>π<sup>0</sup>π<sup>0</sup>, π<sup>±</sup>π<sup>∓</sup>π<sup>0</sup></i>	
<i>η'</i>	<i>(uū + dđ + sš)/√3</i>	0	957.6	3 × 10 <sup>-21</sup>	<i>ηππ, ρ<sup>0</sup>γ</i>	
<i>D<sup>±</sup></i>	<i>cđ, dē</i>	+1, -1	1869	9 × 10 <sup>-13</sup>	<i>Kππ</i>	
<i>D<sup>0</sup>, D̄<sup>0</sup></i>	<i>cū, uē</i>	0, 0	1865	4 × 10 <sup>-13</sup>	<i>Kππ</i>	
<i>F<sup>±</sup></i> (now <i>D<sup>±</sup></i> )	<i>cš, sē</i>	+1, -1	1971	3 × 10 <sup>-13</sup>	not established	
<i>B<sup>±</sup></i>	<i>uđ, bū</i>	+1, -1	5271	14 × 10 <sup>-13</sup>	<i>D + ?</i>	
<i>B<sup>0</sup>, B̄<sup>0</sup></i>	<i>dđ, bđ</i>	0, 0	5275			
<i>η<sub>c</sub></i>	<i>cē</i>	0	2981			6 × 10 <sup>-23</sup>

**VECTOR MESONS (Spin 1)**

Meson	Quark content	Charge	Mass	Lifetime	Principal decays
<i>ρ</i>	<i>uđ, dū, (uū - dđ)/√2</i>	+1, -1, 0	770	0.4 × 10 <sup>-23</sup>	<i>ππ</i>
<i>K*</i>	<i>uš, sū, dš, sđ</i>	+1, -1, 0, 0	892	1 × 10 <sup>-23</sup>	<i>Kπ</i>
<i>ω</i>	<i>(uū + dđ)/√2</i>	0	783	7 × 10 <sup>-23</sup>	<i>π<sup>±</sup>π<sup>∓</sup>π<sup>0</sup>, π<sup>0</sup>γ</i>
<i>φ</i>	<i>sš</i>	0	1020	20 × 10 <sup>-23</sup>	<i>K<sup>±</sup>K<sup>∓</sup>, K<sup>0</sup>K<sup>0</sup></i>
<i>J/ψ</i>	<i>cē</i>	0	3097	1 × 10 <sup>-20</sup>	<i>e<sup>+</sup>e<sup>-</sup>, μ<sup>+</sup>μ<sup>-</sup>, 5π, 7π</i>
<i>D*</i>	<i>cđ, dē, cū, uē</i>	+1, -1, 0, 0	2010	>1 × 10 <sup>-22</sup>	<i>Dπ, Dγ</i>
<i>T</i>	<i>bđ</i>	0	9460	2 × 10 <sup>-20</sup>	<i>τ<sup>+</sup>τ<sup>-</sup>, μ<sup>+</sup>μ<sup>-</sup>, e<sup>+</sup>e<sup>-</sup></i>

More information available from the Review of Particle Physics:

<http://www-pdg.lbl.gov/>

# Summary

Anti-particles for every particle - required by QM+special relativity.

Feynman diagrams - powerful tool for particle interactions.

Three families of leptons and quarks.

Hadrons formed from quarks.

Three forces in the Standard Model of particle physics.